PHYC - 505: Statistical Mechanics Homework Assignment 5

Due March 25, 2014

1. Pathria 4.10 A surface with N_0 adsorption centers has $N(\leq N_0)$ gas molecules adsorbed on it. Show that the chemical potential of the adsorbed molecules is given by

$$\mu = k_B T \ln \frac{N!}{(N_0 - N)a(T)}$$

where a(T) is the partition function of a single adsorbed molecule. Solve the problem by constructing the grand partition function as well as the partition function of the system. [Neglect the intermolecular interaction among the adsorbed molecules.]

2. Pathria 4.13 Define a quantity J as

$$J = E - N\mu = TS - PV$$

Show that for a system in the grand canonical ensemble

$$\overline{\left(\Delta J\right)^2} = kT^2C_V + \left\{\left(\frac{\partial U}{\partial N}\right)_{T,V} - \mu\right\}^2 \overline{\left(\Delta N\right)^2}$$

3. Read the Boltzmann equation material posted on the course website (in the "Excerpts from Books" section), thoroughly understand it, and rewrite in a single page in your own words what is presented there. This is to ensure that you really do that reading assignment.